

1. Detecting your first Community Structure

To detect communities, you can use the `cdlib` package. It also contains functions for evaluation and comparison of partitions. For details, check the documentation at <https://cdlib.readthedocs.io/en/latest/>

If for some reason you cannot install it, you can use the `louvain_communities` function from `networkx`, and `NMI` function from `sklearn`, although you will need to do some transformations.

- (a) Using `networkx`, load the airport dataset
- (b) Using `cdlib`, detect communities on this network using the louvain method. You have to use the `algorithms.louvain` method (and do `from cdlib import algorithms` before).
- (c) Visualize the communities found. In order to interpret them, you should draw each node at its geographical location, with a color per community.

There are several ways to draw a spatial network with colors corresponding to communities, from using Gephi to plotting points on an interactive map using `folium`. Here, I provide a simple code to plot the data as a simple scatter plot

```
import seaborn as sns
import matplotlib.pyplot as plt
x= list(nx.get_node_attributes(g, "lon").values())
y= list(nx.get_node_attributes(g, "lat").values())

coms_dict=coms.to_node_community_map()
hues=list(coms_dict[n][0] for n in g.nodes())

plt.figure(figsize=(12,8))
sns.scatterplot(x=x,y=y,hue=hues,palette=sns.color_palette(
"tab20",len(coms.communities)),s=5)
```

- (d) Vary the resolution parameter and observe changes in the community structure.

2. Comparing Partitions

- (a) The provided airport data also contains information about the country of each airport, which can be interpreted as a *ground truth* partition of the network. You can obtain it using `nx.get_node_attributes(g, "country")`. Transform this information into a `NodeClustering` object of `cdlib` (`nc = NodeClustering(partition, graph, "GroundTruth")`, with `partition` a list of list of nodes).
- (b) Compute the AMI, NMI, or another similarity score (<https://cdlib.readthedocs.io/en/latest/reference/evaluation.html>) between the community structure and the partition in countries
- (c) By exploring with a for loop the values of the resolution parameter for modularity, find the partition with the highest similarity to the partition in countries.
- (d) Compare visually the results, and try to interpret it. Is the partition in country a meaningful topological partition, i.e., is studying this network by considering that nodes in a same country form a coherent/homogeneous group a good approach? (yes and no, probably...)

3. Understanding Modularity. To be sure that you understand correctly the modularity, write a function that compute it for a given partition and a given graph (you can start with a small graph, for instance the `karate_club_graph` of `networkx`). Make your code efficient by remembering that the score depends only on pairs of nodes inside communities. Check that you obtain the same results than using the `cdlib` function `newman_girvan_modularity`. (Be careful that if your network has weights, by default they are used by `cdlib` modularity)
4. Other methods
 - (a) Run the `kclique` algorithm, with `k=10`.
 - (b) Check the communities obtained (if you plot them, be careful that there can be one node belonging to several communities)
 - (c) Identify the nodes belonging to several communities.
 - (d) *optional, infomap might be hard to install on some local configurations*: Install the `infomap` additional package (`pip install infomap wurlitzer`). Run it and compare the communities found with the one found with `louvain`, in term of community sizes and in term of similarity to the country ground truth
5. Internal evaluation
 - (a) Using countries as ground truth does not makes much sense. To evaluate which partition is the most interesting, we can evaluate them with internal scores. You can check <https://cdlib.readthedocs.io/en/latest/reference/evaluation.html#internal-evaluation-fitness-scores> to see the ones available in `CDlib`.
 - (b) Check the `conductance` definition, and then compute it on your different solutions. Check the communities of highest and lowest conductance, and the average conductance for each partition
 - (c) Do the same with the `avg_transitivity`.
 - (d) Draw a scatterplot, in which the `x` axis corresponds to conductance score, `y` corresponds to `avg_transitivity`, and each point is a community. You can compare two methods, by using different colors for communities from different methods.
6. Going further: Intuitions on the SBM

I propose this exercise using only `networkx` and `cdlib`. You could do much more with SBM using `graph-tool` package (real SBM inference, degree-corrected SBM, Hierarchical SBM, etc.), but it requires a little bit more time to get used to at first, so I recommend it only if you're particularly interested in the topic.

- (a) Starting from a reasonable partition of the graph (i.e., countries or the result of the `infomap` method..) Compute the block matrix. You thus need to count the number of edges between and inside each community.
- (b) Using `networkx` `stochastic_block_model` method, generates a graph based on the computed block matrix
- (c) Using the network and node descriptors that you know, compare the properties of this generated graph with the properties of your original graph (and with a simple ER or configuration model). How is it different? How is it similar? Think about clustering coefficient, average distance, distribution of node centralities, degree distribution, internal transitivity, etc.
- (d) How do these properties change when you increase/decrease the number of blocks?