Clustering

# 1 Fundamentals

1. Clustering: getting started
   (a) Download the clustering datasets from the class webpage. Load the first one.
   (b) Using sklearn library, apply `KMeans` algorithm on the dataframe, with 2 clusters, on the numerical columns. You can check the documentations to see how to do it, it should be something like `clusters = KMeans(n_clusters=2).fit_predict(df[["weight","diameter"]])`.
   (c) Add the clusters as a column "cluster" to the dataframe
   (d) To observe the clusters, we can plot (with `seaborn` library for instance, `sns.scatterplot`) with dot colors corresponding to clusters (hue="cluster"). Compare with using the `fruit` information as colors. It should correspond to your intuition.
2. Limits of k-means
   (a) Do the same with the second example. The result should not be as expected. Do you understand why?
   (b) Normalize the data, and retry.
   (c) Do the same with the next example. The result should not be as expected. Do you understand why?
   (d) Try to solve the issue using Gaussian Mixture (class `BayesianGaussianMixture`. Check the `covariance_type` parameter.
   (e) Also try the DBscan approach
   (f) Do the same (comparing ground truth, k-means, GM, DBScan) on the other examples. Every time, try to understand why each of the method succeed or fail. Try to play with the parameters to make the methods succeed.
3. Interpreting clusters
   (a) We want to describe the clusters obtained. Switch back to the synthetic car dataset we used in the first class. Use k-means with 3 clusters.
   (b) Compute the centroid (mean values for each feature), and the size for each cluster. A flexible way to proceed is to extract the clusters (`fit_predict`), add the resulting list as a new column (e.g., "cluster") in a copy of the feature dataframe, then compute statistics by cluster in that dataframe, for instance with `.groupby("cluster").agg(['mean',"count"])`
   (c) If you had to give a manual label to those clusters, to describe the cars they contain, what would it be ? (e.g.: "large and old expensive cars"...)
4. Evaluation and number of clusters
   (a) Compute the silhouette score using method `silhouette_visualizer` from package `yellowbrick`, plot the silhouette score and interpret it.
   (b) We would like to find the optimal number of clusters. Apply the silhouette score method: plot the relation between $k$ and the silhouette score, and search for a maximum value, or a value where there is a "summit" (good luck).

# 2 Going Further

(a) Using this knowledge, explore the proposed Wine dataset: `https://www.kaggle.com/datasets/harrywang/wine-dataset-for-clustering`