EXPLICABILITY/XAI

INTUITION

- Principle: Using supervised machine learning to better understand a dataset
- Correlation: if X increases, Y increases
 - Supervised ML: How X can be used to predict Y
 - =>Extract from the model the relation between X and Y
 - => Take into account also interactions with other variables

INTUITION

- Two aspects of interpretability
 - ▶ I) Feature Importance
 - How much X impacts Y?
 - 2) Nature of the relation
 - When X increases, how does Y change?
 - In general?
 - For a particular observation?
 - Depending on another variable?

Example

- The price of an apartment may depend on the floor
 - Negative relation for low values and positive for high values
 - Depends on the value of the variable "Elevator"
 - For a particular appartment (beutiful view...), a particular relation.

- Interpretable methods
 - Linear/Logistic regressions
 - Lasso
 - Decision tree (small)
 - K-NN
 - **...**
- Black boxes
 - Random forests/XGBoost, etc.
 - Deep Neural Network
 - **...**

- Example: Linear regression
 - ▶ The coefficients == explain relation between variables and target
 - More powerful than correlation coefficient (take other variables into account)
 - Smoking causes cancer. Old people smoke less. Old people have more cancer
 - =>Simple correlation: smoking has little effect on cancer, or even negative correlation
 - =>Linear regression parameters: smoking increases cancer, age increases cancer
 - Variable importance/impact ?
 - /!\ Be careful to raw values!
 - I cigarette increases cancer rate by...
 - I year increases cancer rate by...
 - Not comparable
 - =>Normalize the variables
 - Then you can compare the coefficient values

- Decision tree/Regression Tree
 - Relation variable/Target:
 - Can be read in the tree
 - =>If the building has an elevator, then... else...
 - Feature importance
 - Computed from the gain in the objective
 - => sklearn: tree.feature_importances

· Computing feature importance in a tree

$$FI(f) = \sum_{n \in N(f)} \frac{N_n}{N} \Delta I_n$$

- N(f): set of internal nodes splitting on feature f
- N_n number of training samples reaching node n
- N total number of samples
- ΔI_n Objective decrease produced by that split (RMSE, Gini, etc.)
- Can be normalized to sum to I

AGNOSTIC FEATURE IMPORTANCE

Permutation Feature Importance

AGNOSTIC METHODS

- Evaluating feature importance even in black-box models
 - Independent of the ML algorithm
- · Global score, all cases together

PERMUTATION FEATURE IMPORTANCE

- Intuition: If a variable is important for a model, removing it reduces the performance of the model
 - Feature importance == how much performance is lost without this feature?
- How to remove the feature without changing the model?
 - Randomize the values of the feature
- Score: $FI_j = s(f(D)) s(f(D\pi_j))$
 - s: scoring function
 - f: ML model
 - D: dataset
 - $D\pi_j$: Dataset with variable j randomized



MOTIVATION

- Statistical Modeling: The Two Cultures
 - L. Breiman (2001), Statistical Science,
- · Historically, in data analysis, two cultures
 - Model-based: we assume data follows some statistical model
 - Interpretable methods,
 - Limited complexity
 - A priori on the data (human intuition)
 - Algorithmic/ML
 - Focus on prediction accuracy
- XAI: uniting the two

XAI

• Field concerned with making outcomes yielded by black box models interpretable

Motivations:

- Naturally interpretable models are usually more "naive", have lower capacity of expression
 - =>We want to keep the full power of black-box methods, while being able to explain decisions
 - => e.g.: European Union directive: Al models used to take decision must be able to explain that decision
- To understand relations between variables:
 - If the relation is really complex, the simplified version by a more naive method will be les accurate.

- LIME = Local Interpretable Model-agnostic Explanations
 - Ribeiro, Singh & Guestrin, 2016, KDD
- · Idea: approximate the black box locally by a simple model
 - ightharpoonup Explain the decision for instance x_0
 - For one apartment x_0 , the model answered Y.
 - => What was the role of each variable in this decision?
 - =>For instance: for this apartment, the floor played a positive role...

- · Principle: Builds a surrogate model, valid locally
 - Surrogate model: A simpler model (linear regression, decision tree) that mimic the behavior of the complex model
 - Fitted to predictions of the model, not to real data
 - Intuition: In the solution space, we need a complex model (elevator/no elevator, each city, old/new buildings...)
 - => But locally (e.g., Haussmanian bulding in Paris with no elevator), the model can be well approximated by a simpler one

- Local model behavior approximation
 - Generate random, synthetic points
 - Random perturbations of the point of interest
 - Approximate with a simple model
 - e.g., linear regression
 - Use a loss weighted for proximity
 - More similar points count more

- argmin_g $L(f, g, \pi x_0) + \Omega(g)$
 - g: local surrogate model
 - f: model to approximate
 - L: local loss
 - πx_0 : Locality kernel: control the similarity of sampled points
 - \bullet $\Omega(g)$: complexity penalty (keep the model simple, regularization)

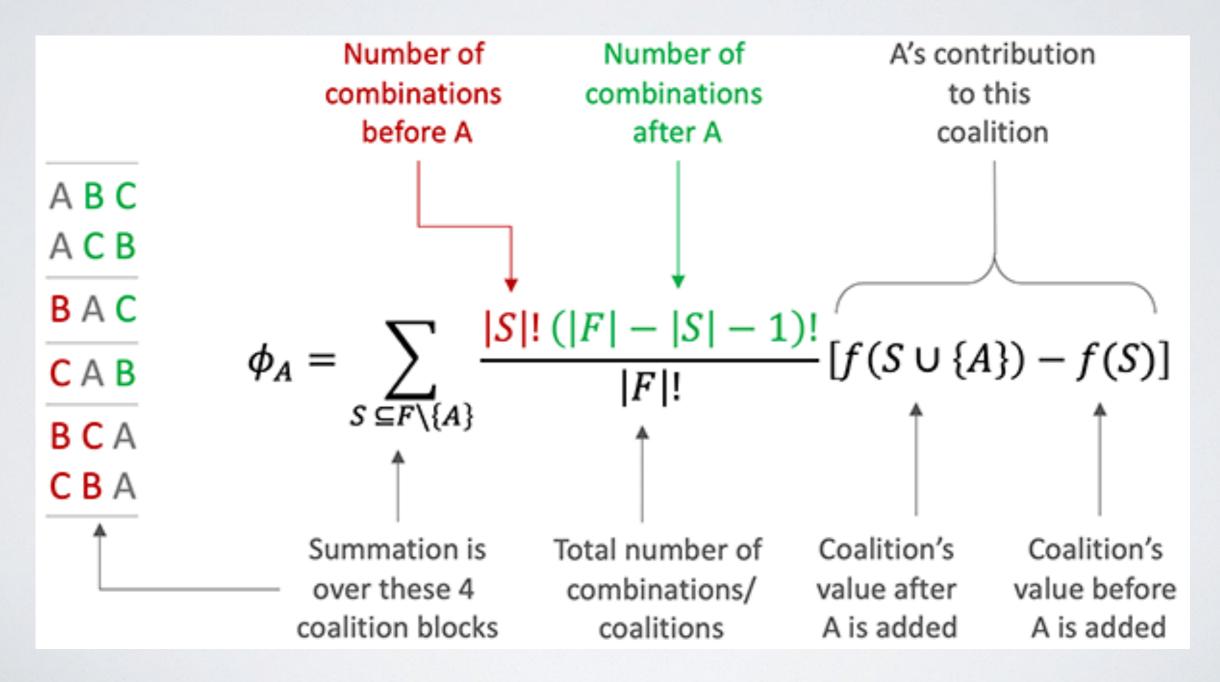
- Surrogate model:
 - A linear or logistic regression model
 - A tree of small size
- Regularized, custom loss for weighting more the less perturbated points
- · The model can be interpreted as usual

- SHapley Additive exPlanations
 - Lundberg & Lee, 2017, NeurlPS: "A Unified Approach to Interpreting Model Predictions"
- Principle:
 - Local estimate (for one prediction)
 - Observe how much each feature changes the outcome when it is added to a subset of other variables
 - Adding age to predict cancer change has different effect if we already include smoking or not

$$\phi_i(x) = \sum_{S \subseteq F \setminus \{i\}} \frac{|S|!(|F| - |S| - 1)!}{|F|!} \left[f_{S \cup \{i\}}(x_{S \cup \{i\}}) - f_S(x_S) \right]$$

- F: set of all features
- $S \subseteq F \setminus \{i\}$: subset of features without feature of interest i ("coalition")
- $f_S(x_S)$: model output when using only features in S
- $f_{S \cup \{i\}}(x_{S \cup \{i\}})$: model outcome when using features in S and i
- $\phi_i(x)$: SHAP value for variable i for observation x
- The large term with factorials is just a weighting to account for multiple possible combinations leading to the same case

Compute effect of variable A

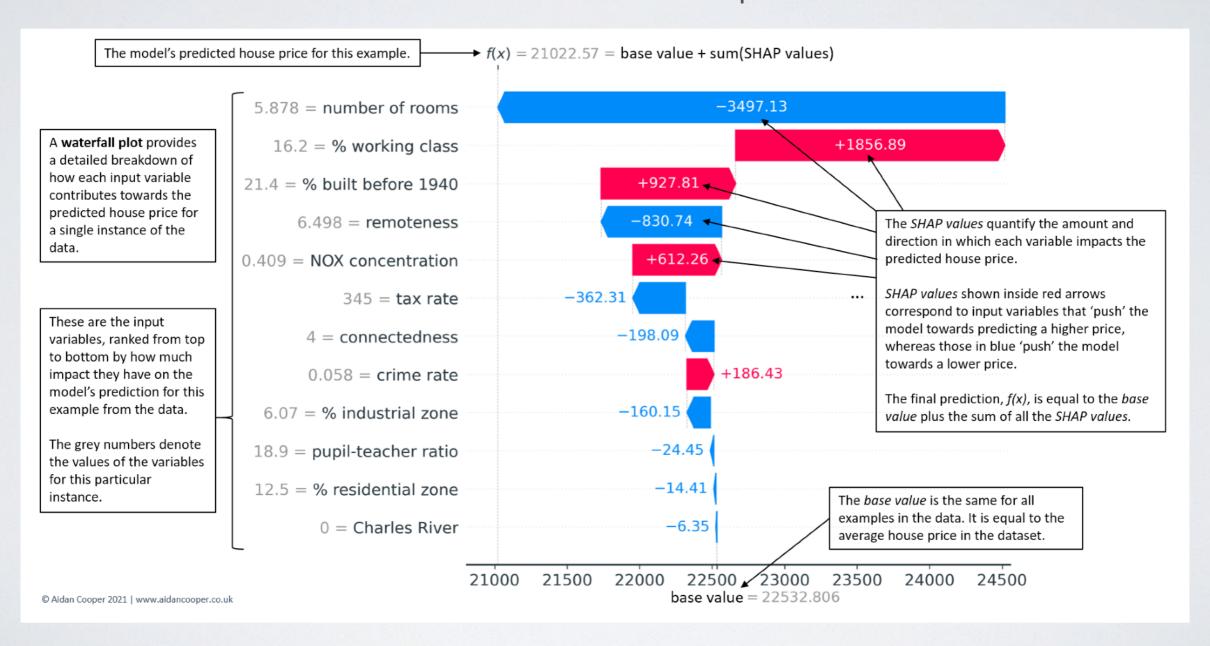


• In practice:

- Removing variables means replacing original values with random values (e.g., taking values at random in the dataset for this variable)
- High complexity: impossible to compute in full in practice
 - Approximate by sampling

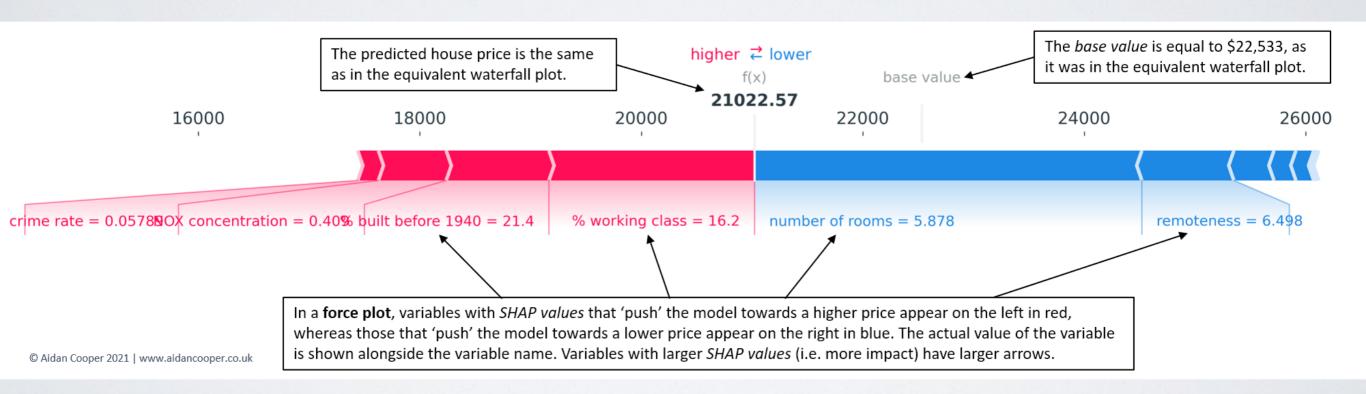
- Four axioms of SHAP
 - Efficiency: Total of all feature contributions equals the actual model output
 - Symmetry: If two features contribute identically, they get identical SHAP values
 - **Dummy:** If a feature never changes the outcome, then it gets SHAP value $\phi_i = 0$
 - Additivity: if two models f,g are combined linearly (h=f+g), then $\phi_i(h)=\phi_i(f)+\phi_i(g)$

Individual instance explanation

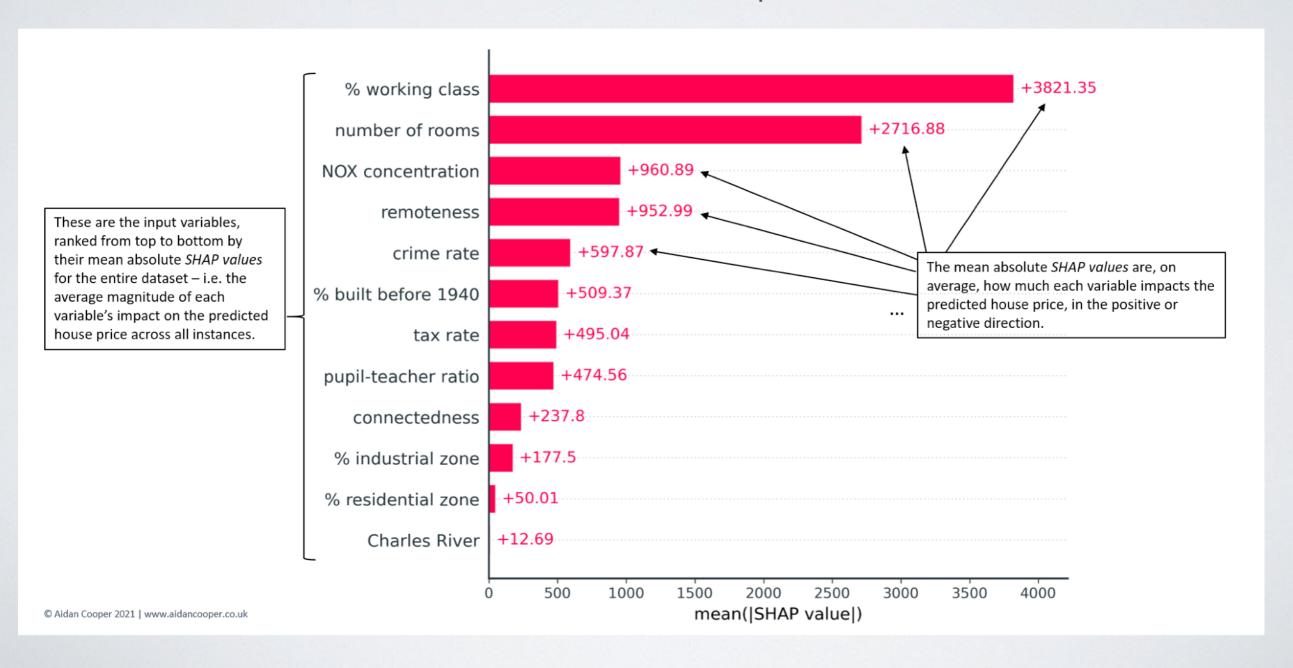


https://www.aidancooper.co.uk/a-non-technical-guide-to-interpreting-shap-analyses/

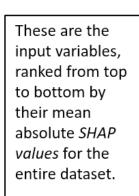
Individual instance explanation



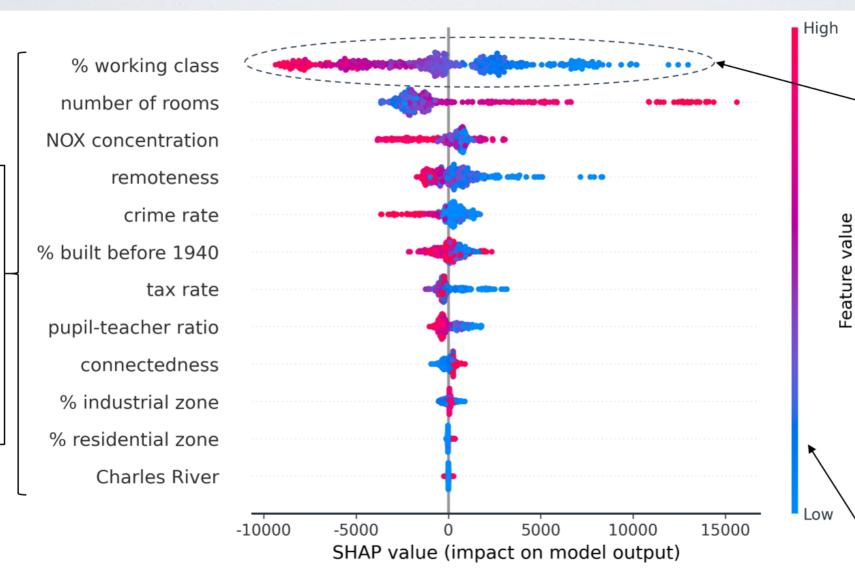
Global feature importance



Beeswarm plot



Note: this ranking is exactly the same as for the bar plot.



In a **beeswarm plot**, for each variable, every instance (i.e. row) of the dataset appears as it's own point. The points are distributed horizontally along the *x*-axis according to their *SHAP* value. In places where there is a high density of *SHAP values*, the points are stacked vertically.

Examining how the SHAP values are distributed reveals how a variable may influence the model's predictions.

The colour bar corresponds to the raw values (not to be confused with the *SHAP values*) of the variables for each instance (i.e. point) on the graph.

If the value of a variable for a particular instance is relatively high, it appears as a red dot. Relatively low variable values appear as blue dots.

Examining the colour distribution horizontally along the *x*-axis for each variable provides insights into the general relationship between a variable's raw values and its *SHAP values*.

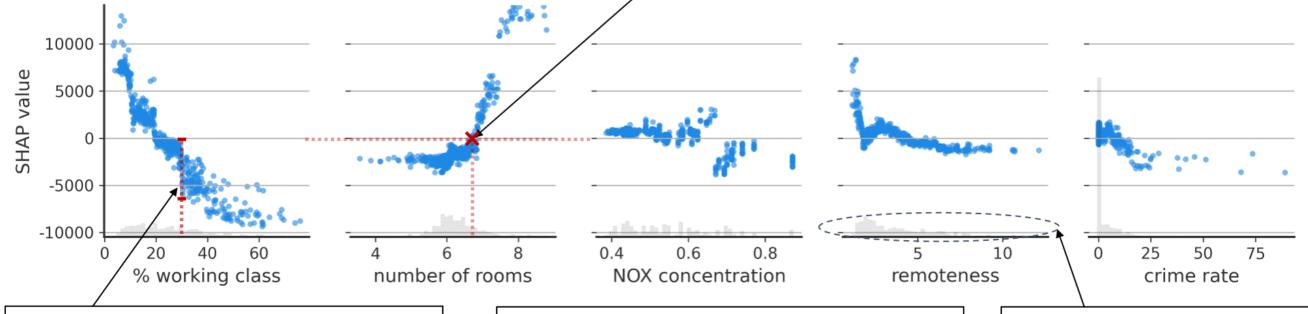
© Aidan Cooper 2021 | www.aidancooper.co.uk

Dependence plot

In a **dependence plot**, every instance (i.e. row) of the dataset appears as it's own point. The points are presented as a scatterplot of a variable's *SHAP values* versus the variables underlying raw values.

SHAP values above the y=0 line lead to predictions of higher house prices, whereas those below it are associated with lower house price predictions. The raw variable value at which the distribution of SHAP values cross the y=0 line tells you the threshold at which the model switches from predicting lower to higher house prices. For number of rooms, this is at approximately 6.8 rooms, as marked by the \times .

With all five plots on the same *y*-scale, the extent of the vertical distribution of the *SHAP values* indicates how much relative influence each variable has on predictions. *% working class* has a much wider range of *SHAP values* than *crime rate*.



The vertical spread of *SHAP values* at a fixed raw variable value is due to *interaction effects* with other variables. For example, here we see that houses with a *% working class* of 30% can have *SHAP values* that range from \$0 to -\$6,500 depending on the other data for those particular instances.

The shapes of the distributions of points provide insights into the relationship between a variable's values and its *SHAP values*. For % working class, we see a negative, linear relationship across the full range of variable values. For number of rooms, we see that *SHAP values* are mostly flat between 4 and 6.5 rooms, but then increase sharply for higher room counts.

The inset histograms just above the x-axis display the distributions of raw variable values. We should be cautious not to overinterpret regions of the dependence plot where the underlying data is sparse (e.g. *crime rates* over 25%).

Interaction plot

