

1 Fundamentals

1. Clustering: getting started
 - (a) Download the clustering datasets from the class webpage. Load the first one.
 - (b) Using sklearn library, apply `KMeans` algorithm on the dataframe, with 2 clusters, on the numerical columns. You can check the documentations to see how to do it, it should be something like `clusters = KMeans(n_clusters=2).fit_predict(df[["weight", "diameter"]])`.
 - (c) Add the clusters as a column "cluster" to the dataframe
 - (d) To observe the clusters, we can plot (with `seaborn` library for instance, `sns.scatterplot`) with dot colors corresponding to clusters (hue="cluster"). Compare with using the `fruit` information as colors. It should correspond to your intuition.
2. Limits of k-means
 - (a) Do the same with the second example. The result should not be as expected. Do you understand why?
 - (b) Normalize the data, and retry.
 - (c) Do the same with the next example. The result should not be as expected. Do you understand why?
 - (d) Try to solve the issue using Gaussian Mixture (class `BayesianGaussianMixture`). Check the `covariance_type` parameter.
 - (e) Also try the DBscan approach
 - (f) Do the same (comparing ground truth, k-means, GM, DBScan) on the other examples. Every time, try to understand why each of the method succeed or fail. Try to play with the parameters to make the methods succeed.
3. Interpreting clusters
 - (a) We want to describe the clusters obtained. Switch back to the synthetic car dataset we used in the first class. Use k-means with 3 clusters.
 - (b) Compute the centroid (mean values for each feature), and the size for each cluster. A flexible way to proceed is to extract the clusters (`fit_predict`), add the resulting list as a new column (e.g., "cluster") in a copy of the feature dataframe, then compute statistics by cluster in that dataframe, for instance with `.groupby("cluster").agg(['mean', "count"])`
 - (c) If you had to give a manual label to those clusters, to describe the cars they contain, what would it be ? (e.g.: "large and old expensive cars"...)
 - (d) Check the difference with and without normalization, and with at least 2 methods.
4. Evaluation and number of clusters
 - (a) Compute the silhouette score using method `silhouette_visualizer` from package `yellowbrick`, plot the silhouette score and interpret it.
 - (b) We would like to find the optimal number of clusters. Apply the silhouette score method: plot the relation between k and the silhouette score, and search for a maximum value.

2 Going Further

- (a) Using this knowledge, explore the proposed Wine dataset: <https://www.kaggle.com/datasets/harrywang/wine-dataset-for-clustering>